# DIGITAL DEEP-SEA SOUNDING LIBRARY

# **DESCRIPTION AND INDEX LIST**

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# ABSTRACT

Automated access to a worldwide coverage of over 1 000 000 deep sea soundings is provided by a new digital data library. The deep sea soundings recorded on available master plotting sheets of the major maritime nations have been incorporated in this new facility.

The methods used in evaluating, digitizing, and processing the data are described in detail. The data are maintained in full both on magnetic tape and on over 60 000 frames of microfilm. The four master library lists are described and sample pages reproduced. The locations of all recorded sound profiles are presented in 708 computer generated index maps.

The data in the library will now be put to use in the solution of numerical problems of both global and regional character. Some of the applications in which this library will be employed include the determination of an average ocean depth model for numerical computations of global geophysical character (such as needed, for example, in the study of ocean tides, the propagation of tsunamis, in geodesy in general, and in the spherical harmonic analysis of earth topography), quantitative textural analysis of topography (slopes, wave lengths, amplitudes), and detailed hypsometric studies.

Automated access to a worldwide coverage of deep sea soundings is needed for many geophysical, geological and cartographical applications. It is the purpose of this paper to give a general account of the data incorporated in a recently established digital data library, to outline the

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methods used in digitizing, processing, and evaluating this data, and to indicate some of the applications in which this library will be employed.

Deep-sea soundings were first obtained by hemp and later by wire line, but since the 1920's virtually all have been obtained by echo timing methods. The echo times collected in the data libraries of the U.S. Naval Oceanographic Office, the Woods Hole Oceanographic Institution, the Scripps Institution of Oceanography, the Lamont Geological Observatory and other oceanographic institutes are recorded in units of 1/400 sec. This unit is known as the standard unit  $(t_e)$ , or the nominal fathom. The echo times shown on plotting sheets maintained by the British Commonwealth hydrographic departments are indicated in approximate fathoms and include a correction for the vertical velocity of sound. Such corrections are made according to a standard table, and may be as large as 300 fathoms. The resulting velocity corrected depths are not strictly true, due to imperfections in the tables, seasonal variations and other factors.

In addition to these two general procedures, individual institutions or individual workers throughout the world have introduced other units of echo time equal to 1/420, 1/750, and 1/725 sec., and have adopted tables other than the standard one to obtain " corrected depths ". Since all echo soundings are measurements of time, one must have accurate information concerning the units and corrections applied and the type, scale, and ultimate accuracy of the recorder used, in order to combine soundings obtained from various sources.

The standard deep-sea plotting sheets use a Mercator grid at either 4 inches or 8 inches to 1° longitude. Other scales and even other projections are employed by various institutions. Since a great variety of units and scales are employed, the compilation of soundings accumulated from various sources has required the expenditure of much effort. The recent significant increase in deep-sea survey and exploration and the installation of digital acquisition systems on survey ships obviously require the use of more efficient automated methods of data processing the correction in order to combine the new data and the older information.

The soundings contained on the master plotting sheets for deep-sea soundings maintained by the U.S. Naval Oceanographic Office, the Lamont Geological Observatory, the hydrographic departments of the United Kingdom, South Africa, Australia, New Zealand, the Netherlands and Germany have been used as the basic source information for a digital library.

Each sounding line was inspected for completeness and accuracy of position and depth, and a rating assigned based on general quality. Precision depth measurements accurate to 1 standard unit  $(t_e)$ , located by precision methods accurate to better than 1 nautical mile and recorded on charts with a spacing between soundings of no more than 2 miles were given the highest rank. Soundings of unknown origin, scattered soundings, and soundings of known origin where accuracy was less than 100  $t_e$  or spacing more than 15 miles, were in general not included in the library.

Soundings were recorded on punched cards by operators employing recently-developed semi-automatic instruments known as digitizers. (Such devices are manufactured by Gerber, Benson-Lehner, and Auto-Trol). In this procedure, the recording head was set over the sounding to be read from the plotting sheet. Each depth value was punched by operating a keyboard and the coordinates recorded automatically by depressing a switch. The precision of the instrumentation for recording the coordinates is 0.001 inch.

The coordinates and depth values are recorded on punched cards by means of a standard IBM card-punch that is connected to the digitizing equipment. Allowing five digits for each of the coordinates of a sounding and its depth value, a maximum of five soundings may be listed on a standard 80-column punch card. The column following each group of fifteen digits (for coordinates and depth) is left empty and serves as an ignore option in cases of error.

This process results in three pieces of digitized information :

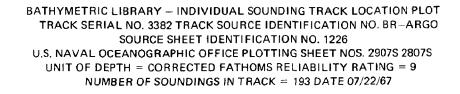
- (1)  $c_x$ , the linear distance from the map origin to the location of the sounding in the x-direction of the map;
- (2)  $c_y$ , the linear distance from the map origin to the location of the sounding in the y-direction of the map;
- (3) The sounding in units of echo time.

The map distances  $c_x$  and  $c_y$  recorded by automatic means must be transformed into geographical coordinates  $X_1$  and  $Y_1$ , by taking into account the map scale and the geographical coordinates of the origin,  $X_0$  and  $Y_0$ . The computational procedure for this is summarized in Appendix A. The computations were performed initially on an IBM 7094 computer, and later on an IBM system/360, Model 75.

Since the whole process is subject to human error, verification is imperative. It is possible to perform all digitizations twice, preferably by two different operators. Two sets of digitized data may be checked one against the other for mutual agreement within predetermined limits of tolerance. Verifying can be done automatically on an electronic computer. For a quick check on position errors, the tracks are plotted either at a reduced scale, or at the original scale, and inspected for errors (figure 1a). By examining computer-plotted vertical profiles (figure 2b), gross discrepancies and inconsistencies were eliminated. Position plots and profiles of the digitized tracks were generated with the aid of a cathode ray recorder (S-C 4020). This device is peripheral to the computer and reads computergenerated magnetic tape from which it produces the plots and depth profiles on  $7.5 \times 7.5$  inch frames. Position plots and vertical profiles of all tracks are incorporated in the bathymetric library.

The results of the recording, after verification and correction, are stored on magnetic tape. For each recorded sounding, the following data are available :

- (1) Coordinates latitude and longitude.
- (2) Echo time depth as listed on source sheet and units of measurement.
- (3) Source sheet number.
- (4) Source track documentation number.
- (5) Source country.
- (6) Reliability rating.



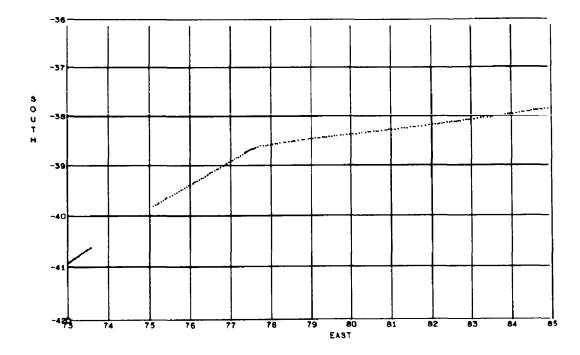


FIG. 1a. — Sample page of master list No. 1 : Individual sounding track location plot.

Echo time depths are inserted in the library in the units in which they are given in the source material. These are, for data from U.S. sources, standard units  $(t_e)$ , i.e. units of 1/400 sec. travel time. Soundings from other source material are given in metres or fathoms, approximately corrected for the velocity of sound according to Matthews' tables [1]. Soundings in other units have not yet been incorporated in the library.

The soundings contained in the library are grouped into track segments. Presently there are 8 375 individual tracks in the library. Each track has been assigned a reliability rating, ranging from 0 to 11. This rating is based on the quality of the echo sounding recording. The factors taken into account for judging the reliability have been the type of echo-sounding equipment used and its resolution, the type of navigation available to the sounding vessel and the associated accuracy, and the density of recordings per unit length of the track (table 1). Sounding tracks have been compiled for 708 plotting areas according to the U.S. Naval Oceanographic Office numbering system. A list is maintained of all tracks in each area including a record of source information, scale, serial number and date entered.

#### DIGITAL DEEP-SEA SOUNDING LIBRARY

BATHMETRIC LIBBORY — INDIVIOUNL SOUNDING TRACK TRACK SERIAL NO. 3382 TRACK SOURCE IDENTIFICATION NO. 6R-AGO SOURCE SHEET IDENTIFICATION NO. 1286 U. S. NAVAL OCEANOGRAPHIC OFFICE PLOTTING SHEET NOS. 28075 28075 UNIT OF DEPTH - CORRECTED FATHOUS RELIABILITY RATING - 9 NUMBER OF SOUNDINGS IN TRACK - 193 DATE 07/22/67

LISTING OF DEPTHS AND COORDINATES OF INDIVIDUAL SOUNDINGS

LAT	LONG	DEPTH	LAT	LONG	DEPTH	LAT	LONG	DEPTH	LAT	LONG	DEPTH	LAT	LONG	DEPTH
40.927 8	73.084 E	1970	30.357 8	76.008 E	1796	38.615 \$	77.563 E	866	30.314 8	3 308.08	1834	37.993 3	83.954 E	1886
40.913 B	73.042 E	1971	39.348 4	74.124 E	1824	38.006 8	77.961 E	772	38.308 8	40.995 C	1805	37.944 1	64.031 E	1965
40.007 8	73.062 E	1976	39.323 \$	78.168 E	1705	34.996 8	78.043 E	471	30.306 8	81.011 E	1841	37.974 8	84.121 E	2036
40.884 8	73.002 E	2002	39.303 \$	78.224 E	1776	38.590 8	76.006 E	718	30.200 \$	81.084 E	1088	37.966 8	84.197 E	2080
40.873 8	73.112 E	2024	39.261 4	76.268 E	1783	34.543 8	78.155 E	710	30.291 8	81.179 E	1000	37.956 3	84.257 E	2072
40.857 8	73.136 E	2079	30.254 8	78.321 E	1730	34.576 3	78.217 E	805	38.202 8	81.250 E	1912	37.950 8	84.304 E	1879
40.844 8	73.159 E	2005	39.254 8	76.306 E	1718	38.563 8	78.311 E	1005	30.201 8	81.321 E	1880	37.845 8	84.384 E	1936
40.832 8	73.182 E	2128	39.212 \$	78.415 E	1000	30.557 8	78.365 E	1140	30.271 8	81.400 E	1917	37.938 3	84.433 E	1991
40.820 8	73.206 £	2128	30.190 8	78.440 E	1744	36.546 8	78.455 E	1710	38.257 1	01.40E E	1882	37.928 8	84.491 E	1978
40.004 8	73.224 E	2173	39.100 %	76.408 E	1730	34.542 8	78.908 E	005	34.255 1	01.541 E	1934	37.921 8	84.545 E	2032
40.794 8	73.250 E	2050	30.167 8	76.513 E	1748	34.537 8	78.556 E	500	38.249 8	81.590 E	1000	37.910 3	84.597 E	1960
40.783 8	73.271 E	2065	39.146 8	76.500 E	1730	30.528 \$	78.595 E	640	34.240 8	81.679 E	1919	37.910 8	54.648 E	1951
40.770 8	73.300 E	2026	39.125 8	76.613 E	1739	34.520 8	78.682 E	950	34.232 8	81.761 E	1914	37.804 8	\$4.710 E	1906
40.755 8	73.324 E	2034	30.105 8	78.641 E	1726	34.512 8	78.771 E	941	34.222 3	81.845 E	1974	37.006 8	64.760 E	1918
40.744 8	73.349 E	2029	30.D00 %	76.706 E	1696	34.506 8	78.827 E	748	30.213 3	\$1.931 E	1911	37.893 3	84.839 E	1910
40.732 3	73.373 E	2035	39.000 \$	76.757 E	1967	34.495 8	78.916 E	738	30.205 8	84.019 E	1969	37.002 8	84.919 E	1962
40.719 8	73.398 E	2073	30.037 8	76.811 E	1613	30.485 8	78.976 E	620	34.190 1	96.060 E	1914	37.870 8	#5.000 E	1934
40.705 8	73.417 E	2055	39.018 \$	76.855 E	1601	36.485 1	79.038 E	987	38.194 \$	42.154 E	1976			
40.687 3	73.439 E	2024	39.005 8	76.000 E	1505 1613	38.478 8	79.105 E	1002	30.191 8	82.204 E	1964			
40.678 3	73.449 E	2051	38.995 3	76.904 E 76.953 E	1590	38.466 8 38.466 8	79.167 E 79.226 E	1072	30.181 8	42.240 E	1951			
40.668 8	73.464 E	2025	36.992 8		1615	36.460 8	79.200 E	1 202	34.172 8	#2.313 E	1917			
40.652 8	73.514 E	2045 2048	38.942 8 38.960 8	77.001 E	1596	36.456 8	79.335 E	1448	38.166 8	42.398 E	1901			
40.640 3	73.536 E			77.101 E	1500	36.451 8	79.395 E		30.161 8	R2.494 E	1940			
40.628 5	73.556 E	2050	30.007 1 38.070 1	77.151 E	1537	30.447 8	79.450 E	1720	30.153 8 30.147 8	82.906 E 82.972 E	1017			
39.796 3	75.064 E 75.141 E	2021 2020	38.953 8	77.195 E	1518	38.442 \$	79.513 E	1806	34.142 3	82.822 E	1946			
39.780 5	75.141 E	1996	38.827 1	17.244 E	1360	36.436 \$	79.575 E	1825	36.142 8	42.422 E	1911			
39.757 8	75.220 E	1984	38.801 8	77.294 E	1077	36.431 8	79.649 E	1012	34.131 8	42.738 E	1863			
39.734 8	75.200 E	1961	30.782 3	77.339 E	757	36.423 8	79.742 E	1017	30.119 8	92.812 C	1000			
30.711 8	75.334 E	1951	38.767 8	77.359 E	284	30.417 8	79.818 E	1769	30.113 8	62.872 E	1069			
39.664 5	75.379 E	1827	34.756 8	77.384 E	191	38.408 8	79.900 E	1756	34.107 8	82.969 E	1874			
39.661 3	75.426 E	1913	38.743 8	77.417 E	150	36.40E 8	79.950 E	1766	34.104 1	82.976 E	1814			
39.633 8	75.498 E	1847	38.729 8	77.430 E	134	34,394 8	60.038 E	1740	34.098 1	81.070 E	1911			
39.602 8	75.548 E	1787	38.717 8	77.463 E	104	38.388 3	80.131 E	1725	38.D07 8	83.190 E	1831			
39.577 8	75.616 E	1854	38.705 8	77.494 E	62	30.300 8	80.205 E	1764	34.074 8	63.232 T	1061			
38.557 3	75.664 E	1745	38.694 8	77.515 E	49	38.372 8	60.276 E	1793	34.062 8	83.307 E	1057			
39.533 8	75.716 E	1765	38.705 8	77.531 E	22	34.345 8	40.37E E	1761	34.058 8	63.393 E	1841			
39,509 \$	75.744 E	1670	38.694 5	77.564 E	331	34.356 \$	80.429 E	1841	34.053 1	83.481 E	1876			
39.491 3	75.000 E	1725	34.641 8	17.545 E	481	38.354 8	80.487 E	1821	34.045 8	83.530 C	1864			
39.465 3	75.858 E	1827	30.664 \$	77.628 E	560	34.343 8	80.570 E	1767	34.036 5	83.810 E	1964			
39.444 1	75.905 E	1839	30.641 5	77.677 E	737	38.341 8	80.629 E	1841	34.027 5	83.698 E	1007			
39.421 3	75.957 E	1060	34.424 8	77.744 E	666	34.336 8	80.602 E	1787	38.016 8	83.768 E	1454			
39.404 \$	76.002 E	1743	34.427 8	77.810 E	688	38.327 8	80.762 E	1769	38.009 8	83.851 E	1904			
39.378 8	76.007 E	1835	30.414 8	77.863 E	779	38.316 8	80.ME E	1000	37.999 8	83.903 E	1004			
39.376 8	10.037 E	1692	30.414 4											

Fig. 1b. — Sample page of master list No. 1 : Listing of depths and coordinates of individual soundings (for track in Figure 1a).

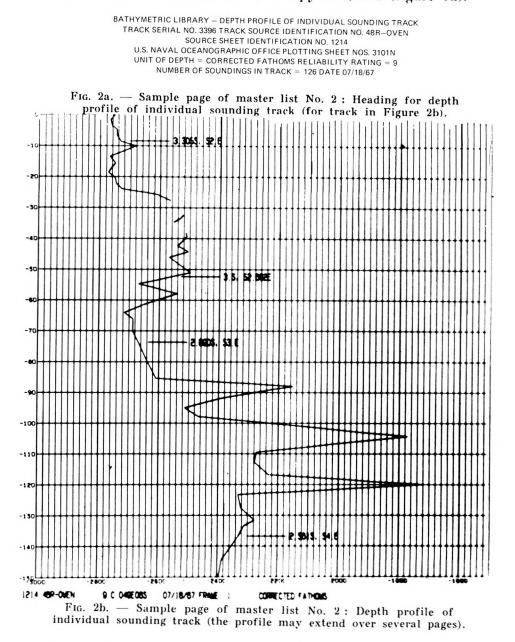
Data from the continuing programs of Lamont Geological Observatory and U.S. National Science Foundation's R/V *Eltanin* is continuously fed into the library, and programs exist so that this can be done on a digital computer. Beginning in 1966, all sounding data acquired by the U.S. Naval Oceanographic Office is routinely digitized according to a system compatible with this library.

For easy availability, the contents of the library are arranged in four master lists. The geographical coordinates (latitude and longitude) and the depth for each individual sounding are presented in master list No. 1. For each track, a sounding location plot is given, as well as a detailed listing of depths and coordinates (see sample pages in figures 1a and 1b). The following information is provided for each track :

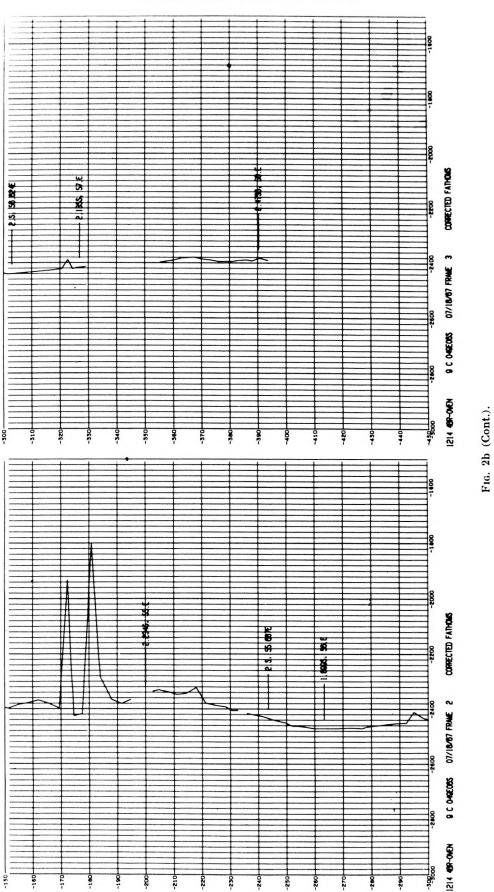
- 1) Track serial number (ranging from 1 to 8 375);
- 2) Track source identification number;
- 3) Source sheet identification number;
- 4) U.S. Naval Oceanographic Office Plotting Sheet Nos. of the areas in which the track is located;
- 5) Unit of echo time depth;

- 6) Reliability rating;
- 7) Number of soundings in the track;
- 8) Date of incorporation into the library.

The entries for each track take up two or more pages : One page for the location plot, and one or more pages for the list of the soundings. The plots have been reproduced in such a manner that 1° longitude on standard U.S. Naval Oceanographic Office plotting sheets is represented by 80 " raster " units of the S-C 4020 CRT recorder used to produce these plots. On standard U.S. Naval Oceanographic Office Plotting Sheets, 1° longitude measures 4 inches. The hard-copy camera of the S-C 4020 instrument records 1023 " raster " units on 7.5 inch. Thus, the reduction in scale from source sheets to the size of hard copy is 1/6.82 (figure 1a).



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# DIGITAL DEEP-SEA SOUNDING LIBRARY

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#### TABLE 1

### Reliability rating for digitized sounding tracks

(1) Precision recorders operated on  $400 t_{e}$  scale, recordings on 18 inch paper or better.

(2) Precision recorders operated on  $> 400 t_s$  scale, or recordings on < 18 inch paper. (3) Non precision recorders operated on  $600 t_s$  scale. (4) Non precision recorders operated on 600 or  $2000 t_s$  scale.

(5) Non precision recorders operated on 2 000, 4 000, or 6 000 t, scale.

(6) Non precision recorders operated on 4 000 or 6 000 t, scale.

(7) Any other recorders.

Reliability rating	Type of echo- sounding equipment	Resolution	Spacing : approximate number of soundings per degree latitude	Type of navigation	Accuracy of navi- gational fixes (mile)
11	(1)	± 1 fm	> 10	Lorac or Decca $\lambda$	± 0.1
10	(1)	± 1 fm	> 10	Loran C, Transit	± 0.5
9	(1)	± 1 fm	> 10	Loran A or Stars	± 2
8	(2)	± 5 fm	> 5	Poor or unknown	>2
7	(3)	± 5 fm	> 10	Stars or better	± 2
6	(4)	± 10 fm	> 10	Stars or better	± 2
5	(5)	± 25 fm	> 10	Stars or better	± 2
4	(6)	± 50 fm	> 10	Poor or unknown	>2
3	(6)	± 50 fm	< 10	Stars or better	± 2
2	(6)	± 50 fm	< 10	Poor or unknown	>2
1	(7)	_	< 5		
0	(7)		< 3	-	-

Depth profiles of each sounding track at 100/1 vertical exaggeration are provided by master list No. 2. The vertical coordinates represent echo time depth in the original units and the horizontal coordinates indicate distance along the track in nautical miles, reckoned from the first recorded sounding. (See sample pages in figures 2a and 2b).

Source sheet information is summarized in master list No. 3 (figure 3). The information for each source sheet recorded on a single page contains the following entries :

- (1) Source sheet identification number (ranging from 1 to 2119);
- (2) Name of source country;
- (3) Scale of source sheet;
- (4) U.S. Naval Oceanographic Office Plotting Sheet Nos. of the areas in which the tracks on this sheet are located:
- (5) Number of tracks on this sheet;
- (6) Number of soundings on this sheet;
- (7) Unit of echo-time depth;
- (8) Date of compilation;
- (9) For each individual track on this sheet :
  - (a) The track serial number:
  - (b) The track source identification number;
  - (c) The reliability rating;
  - (d) Number of soundings in the track;
  - (e) U.S. Naval Oceanographic Office Plotting Sheet Nos. of the areas in which this track is located.

#### BATHYMETRIC LIBRARY – SOURCE SHEET INFORMATION SOURCE SHEET IDENTIFICATION NO. 1266 SOURCE COUNTRY SOUTH AFRICA SCALE OF SOURCE SHEET 1/1000000 AT 46 DEGREES LATITUDE U.S. NAVAL OCEANOGRAPHIC OFFICE PLOTTING SHEET NOS. 3506S 3507S 3406S 3407S 3505S NUMBER OF TRACKS ON THIS SHEET 45 NUMBER OF SOUNDINGS ON THIS SHEET 1697 UNIT OF DEPTH CORRECTED METERS DATE 07/16/67

TRACK	TRACK SOURCE		NUMBER OF	U. S. NAVAL
SERIAL	IDENTIFICATION	QUALITY	SOUNDINGS	OCEANOGRAPHIC OFFICE
NO.	NO.	RATING	IN TRACK	PLOTTING SHEET NOS.
	SA-01402	7	109	35063 35073
4013		7		
4046	SA-02402		47	35068
4010	SA-03402	7	27	35078 35068
4000	SA-04402	7	45	35078 35068
3995	SA-05402	7	26	34078 34068
4005	SA-06402	7	19	35063
3988	SA-08402	7	36	35065
4011	SA-09402	7 7	51	34068
3984	1SA-AFRI	4	49	35068 35078
3985	1 SA-DANA	- 3	8 7	34063
4008	1 SA-01 S2	3		35068
4012	1 SA-METE	7	42	35068 35078
3992	1 SA-NATA	5	34	34063
3994	1 SA-PROT	5	32	35068
3998	1 SA-PTEA	5	42	35068 35058
3987	1 SA-SHAC		11	34078
4016	2SA-AFRI	4	39	3506S
4009	2SA-DANA	3	122	35068
4007	25A-0152		5	3506\$
4002	2SA-HETE	7	28	35078 35068
3991	2SA-NATA	5	55	34068
3996	2SA-PROT	5	7 59	35068 35058 35068
4014	2SA-PTEA	5	30	
4043	2SA-PUMA	5		35068
4004	2SA-SHAC	7	14	34078
4017	3SA-AFRI	3	29 25	35068
4006	35A-0152			35063
4022	3SA-HETE	7	23	35068
3990	3SA-NATA		11	34068
4045	3SA-PROT	5	50	35068
3997	3SA-PTEA	5	47	35069 35058
4003	3SA-SHAC	5	55	34078 34068 35068
4018	4 SA-AFRI	7	29	35068
3989	4 SA-NATA	7	23	34068 35068 35058
4047	4 SA-PTEA	5	16	35063 35073
3986	4 SA-SHAC	5 7	47	
4044	5 SA-NATA		27	34068
4020	5SA-PTEA	5	101	35068
4015	5 SA-SHAC	5	30	35068
3999	6 SA-NATA	7	27	34063
4019	63A-PTEA	5	97	35068
3993	6 SA-SHAC	5	31	35068
4642	7 SA-NATA	7	52	35068
4001	7 SA-PTEA	5	12	35068
4021	8 SA-NA TA	7	21	35068

FIG. 3. — Sample page of master list No. 3 : Listing of source sheet information.

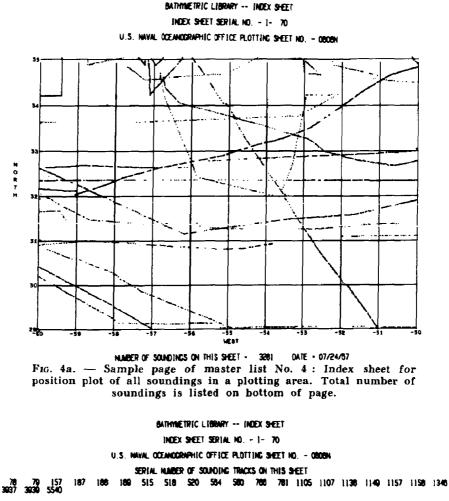
The first page (see sample in figure 4a) of master list No. 4 contains a position plot of all the soundings in a plotting area (figure 5). The second page (see sample in figure 4b) contains a list of the serial numbers of the tracks which include soundings in the area. By referring to master lists Nos. 1 or 2 one may obtain the coordinates or echo time depths of the 

FIG. 4b. — Sample page of master list No. 4 : Serial numbers of sounding tracks on Index Sheet (for sheet in Figure 4a).

soundings along a particular track. The index sheets in this list are designated with the pertinent U.S. Naval Oceanographic Office plotting sheet numbers. They also bear running Sheet Index Numbers.

The four master lists are quite voluminous : list No. 1 comprises about 20 000 pages, list No. 2 about 40 000 pages, list No. 3 about 2 000 pages, and list No. 4 comprises 1 416 pages.

In addition, a magnetic tape with library information has been prepared. This tape contains in digital form the basic data from which the library lists have been constructed. The tape contains the original verified digitizations for each track of soundings. These quantities are  $c_x$  and  $c_y$ , the distances, in digitizer counts of 1/1000 inch, from map origin to the location of the sounding along the coordinate axes, z, the key-punched echo time depth value, and a count number indicating the position of the sounding in the track.

Various FORTRAN programs have been written in connection with the establishment of this data library. For example, one such auxiliary

#### PLOTTING SHEET INDEX

	100'	danation	the second secon	140'			dundantina		140'		120'	100'			60.		20'			20'	40		~	
	0721	N		0621 N		0:	521 N		0421	N		0321 N		0	221 N		0121 1	•		0921 N		08	21 N	
142	ON	1320 N	1220 M	4 II:	20 N	1020 N	0920 N	08	20 N	0720 N	0620 1	4 05	20 N	0420 N	0320	N 0	220 N	0120 N	1820 1	1 17	20 N	1620 N	1520 N	
919 N	1819 N	1719 N	1619 N	1519 N	1419 N	1319 N	1219 N	1119N	1019 N	0919 N	0819 N	0719 N	0619 N	051914	04184	E SSI FN	MIPN	0119 N	2419 N	2319 N	2219 N	2119 N	2019 N	
	TALBAT	1718 N	1618 N	1518 N	1418 N	1318 N	1218 N	1118 N	1018 N	0918 N	0818.N	ARISO	Onle H	OSIEN			0218 N	0118 N	2418	-	2218 N	2118 N	2018 N	-
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FIG. 5. — U.S. Naval Oceanographic Office Plotting Sheet Index.

program inserts or removes corrections for the velocity of sound according to Matthews' Tables [1], selecting also the proper Matthews Area, according to geographical location of the sounding to be corrected.

The index sheets of master list No. 4 have been reproduced in full [5]. Microfilmed copies have been made of all master lists, as well as the library magnetic tape.

# **CONCLUDING REMARKS**

The library was established to satisfy three general needs. The initial motivation stemmed from the need for an average ocean depth model for numerical computations of a global geophysical character. One of the first intended uses of the library will be to compute such an average ocean depth model for use in tidal studies [2]. Such a model is also needed in other dynamic problems of sea motion and the propagation of tsunamis. It will also be useful in geodesy in general, and in the spherical harmonic analysis of earth topography.

The library facility will provide a more efficient method of compiling and plotting soundings recorded in a variety of units, scales, and formats. The variety of charts and vertical profiles required in physiographic studies [3] will be prepared by machine.

A third use relates to quantitative textural analysis of topography (slopes, wave lengths, amplitudes) and to detailed hypsometric studies — subjects now of increasing interest to oceanographers [4].

#### APPENDIX A

#### **Computation of Coordinates on Digitized Maps**

This Appendix summarizes the computational procedure for finding the geographical coordinates of soundings which are digitized from oceanographic plotting sheets. The sheets are in Mercator scale.

It is assumed that the origin for digitization is located at a point  $(X_0, Y_0)$  on the map (figure 6). X and Y are geographical coordinates. X ranges from 0° to 360° in the East direction. Y ranges from 90° at the North Pole through 0° at the Equator to -90° at the South Pole.

It is required to find the geographical coordinates  $X_1$  and  $Y_1$  of a digitized sounding, which is  $c_x$  digitizer counts along the X-axis and  $c_y$  counts along the Y-axis away from the origin.  $c_x$  is counted positive by going eastward, and  $c_y$  is counted positive by going northward from the origin. The resolution of the reading system is r counts per inch of reading head travel for each axis. For the instrumentation used to establish the present data library, r = 1000.

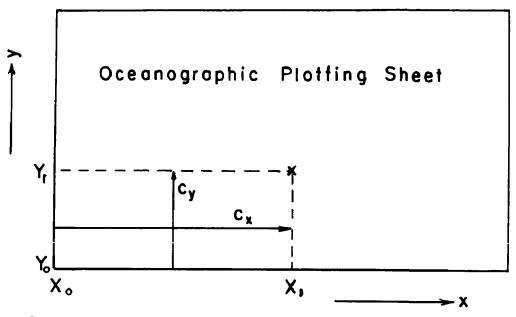


FIG. 6. — Coordinate system for digitization of soundings from oceanographic plotting sheets :  $c_x, c_y$  : distances along axes in digitizer counts

 $c_{s}, c_{y}$  : distances along axes in digitiz X<sub>0</sub>, Y<sub>0</sub> : origin for digitization

 $X_1, Y_1$  : location of digitized sounding.

It is necessary to know the scale of the maps to be digitized. For standard plotting sheets of the U.S. Naval Oceanographic Office, between  $64^{\circ}$  North and  $65^{\circ}$  South (sheets XX01N — XX14N and sheets XX02S — XX14S, where XX ranges from 01 to 36), the distance between meridians,  $1^{\circ}$  apart, is exactly 4 inches. This corresponds to a scale of 1/1093614at the equator. On sheets XX15N — XX19N and sheets XX15S — XX19S the distance between two adjacent meridians, which are  $1^{\circ}$  apart, is 2 inches, corresponding to a scale of 1/2187228 at the equator. If we assign in the computations a scale factor s = 1 for the "standard" U.S. Naval Oceanographic Office plotting sheets between  $64^{\circ}$  North and  $65^{\circ}$  South, then obviously the aforementioned higher latitude sheets XX15 — XX19 have a scale factor s = 0.5. For maps in Mercator scale from other sources the scale factor is determined by

$$s = \frac{1093614\cos\theta}{m} \tag{1}$$

Here  $\theta$  is the latitude at which the map scale 1/m is given.

We now proceed to compute  $X_1$  and  $Y_1$ .

Computation of  $X_1$ :

$$X_{1} = X_{0} + \frac{c_{x}}{4 \cdot r \cdot s}$$
(2)

Computation of  $Y_1$ :

$$Y_{1} = \frac{360}{\pi} \left\{ \arctan \left( e^{\tau_{1}} \right) \right\} - 90$$
 (3)

where

$$\tau_1 = \tau_0 + \frac{c_y}{4.r.s} \cdot \frac{\pi}{180}$$
(4)

and

$$\tau_0 = \ln \tan \left\{ \frac{1}{2} Y_0 + 45 \right\}$$
(5)

if the argument of ln (\*) tan is expressed in degrees, or

$$\tau_{0} = \ln \tan \left\{ \left( \frac{Y_{0}}{360} + \frac{1}{4} \right) \pi \right\}$$
(6)

if the argument of ln tan is expressed in radians.

A modification in the computation of  $Y_1$  is necessary for cases of maps which are linearly subdivided between lines of latitudes. This applies to U.S. Naval Oceanographic Office Plotting Sheets XX01N — XX14N and XX02S — XX14S (the region between 64° North and 65° South). It also applies to oceanographic sheets from other sources, if so indicated. In these cases :

$$Y_1$$
 modified =  $[Y_1] + \frac{\tau_1 - \tau_A}{\tau_B - \tau_A}$  in the Northern Hemisphere (7)

= 
$$[Y_1] - \frac{\tau_1 - \tau_A}{\tau_B - \tau_A}$$
 in the Southern Hemisphere (8)

where

[Y] = Integral part of Y in degrees. (9) $\tau_1 is as defined in equation (4).$ 

$$\tau_{\mathbf{A}} = \ln \tan \left\{ \frac{1}{2} \left[ \mathbf{Y}_{1} \right] + 45 \right\}$$
(10)

if the argument of ln tan is expressed in degrees, or

$$r_{\rm A} = \ln \tan \left\{ \left( \frac{[Y_1]}{360} + \frac{1}{4} \right) \pi \right\}$$
(11)

if the argument of ln tan is expressed in radians.

$$r_{\rm B} = \ln \tan \left\{ \frac{1}{2} \left[ Y_1 \pm 1 \right] + 45 \right\}$$
(12)

if the argument of ln tan is expressed in degrees, or

$$\tau_{\rm B} = \ln \tan \left\{ \left( \frac{[{\rm Y}_1 \pm 1]}{360} + \frac{1}{4} \right) \pi \right\}$$
(13)

if the argument of ln tan is expressed in radians.

In equations (12) and (13), the positive sign is taken for locations in the northern hemisphere, while the negative sign applies to locations in the southern hemisphere.

(\*) ln = Napierian logarithm.

The varying information which has been used to compute  $X_1$  and  $Y_1$ in each specific case for the present holdings of the library is presented in table 2.

# TABLE 2

### Source information for digitized sounding tracks

Legend for Unit of Depth :

t. : echo times in units of 1/400 sec.
 C : corrected fathoms, according to Matthews' Tables

M : corrected metres, according to Matthews' Tables

Source sheet identification No.	Source country	Map source sheet scale 1/m	Latitude for map source sheet scale	Scale factor s	Linear subdivision	Unit of depth
1-177	U.S.	1/1093614	Equator	1	yes	$i_e$
178	U.S.	1/972101	Equator	1.125	yes	$t_e$
179-224	U.S.	1/1093614	Equator	1	yes	$t_e^c$
225-232	U.S.	1/972101	Equator	1.125	yes	$t_e^{\epsilon}$
233-1159	U.S.	1/1093614	Equator	1	yes	$t_e^e$
1160-1188	U.S.	1/2187228	Equator	0.5	no	$t_e$
1189-1220	U.K.	1/1000000	33°	0.917181	yes	Ċ
1221-1231	U.K.	1/1000000	46°	0.759688	yes	C
1232-1240	Australia	1/1000000	46°	0.759688	yes	C
1241-1264	Australia	1/1000000	33°	0.917181	yes	С
1265-1270	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1271-1273	Australia	1/1000000	46°	0.759688	yes	Č
1274-1277	So. Africa	1/1 000 000	46°	0.759688	yes	М
1278-1280	U.K.	1/1000000	57°	0.595625	yes	С
1281-1288	So. Africa	1/1000000	46°	0.759688	yes	М
1289-1294	Germany	1/1000000	46°	0.759688	yes	М
1295-1311	Germany	1/1 000 000	33°	0.917181	yes	М
1312-1319	So. Africa	1/1000000	33°	0.917181	yes	М
1320-1328	U.K.	1/1000000	46°	0.759688	yes	C
1329-1334	U.K.	1/1000000	57°	0.595625	yes	C
1335-1336	So. Africa	1/1 000 000	57°	0.595625	yes	C
1337-1339	So. Africa	1/1 000 000	33°	0.917181	yes	C
1340-1346	U.K.	1/1000000	33°	0.917181	yes	С
1347-1356	Australia	1/1000000	33°	0.917181	yes	С
1357	So. Africa	1/1000000	46°	0.759688	yes	М
1358-1359	So. Africa	1/1000000	46°	0.759688	yes	С
1360	So. Africa	1/1000000	46°	0.759688	yes	М
1361	So. Africa	1/1000000	46°	0.759688	yes	C
1362-1363	So. Africa	1/1000000	46°	0.759688	yes	M
1364-1400	U.S.	1/546807	Equator	2	yes	$t_e$
1401-1447	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1448	U.S.	1/2187228	Equator	0.5	no	$t_e$
1449-1485	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1486-1489	U.S.	1/2187228	Equator	0.5	no	$t_e$
1490-1494	U.S.	1/1093614	Equator	1	yes	$t_e$
1495-1512	U.S.	1/546807	Equator	2	yes	t <sub>e</sub>
1513	Australia	1/1000000	46°	0.759688	yes	č
1514	U.K.	1/1000000	57°	0.595625	yes	C
1515	U.K.	1/1000000	65°	0.462181	yes	С

### TABLE 2 (continued)

### Source information for digitized sounding tracks

Source sheet identification No.	Source country	Map source sheet scale 1/m	Latitude for map source sheet scale	Scale factor s	Linear subdivision	Unit of depth
1516-1523	Ū.K.	1/729076	Equator	1.5	yes	C
1524	Germany	1/306979	Equator	3.5625	yes	М
1525-1526	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1527-1531	<b>U.K</b> .	1/1000000	33°	0.917181	yes	C
1532-1541	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1542-1544	U.S.	1/2187 228	Equator	0.5	no	t <sub>e</sub>
1545-1559	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1560	U.S.	1/2 187 228	Equator	0.5	no	t <sub>e</sub>
1561	Germany	1/1000000	70°	0.374038	no	M
1562-1603	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1604	U.S.	1/2187228	Equator	0.5	no	t <sub>e</sub>
1605-1628	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1629	U.S.	1/2187228	Equator	0.5	no	t <sub>e</sub>
1630-1678	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1679-1682	U.S.	1/2187228	Equator	0.5	no	t <sub>e</sub>
1683-1817	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
1818-1822	U.S.	1/2187228	Equator	0.5	no	t <sub>e</sub>
1823-2033	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
2034	U.S.	1/2187228	Equator	0.5	no	t <sub>e</sub>
2035-2118	U.S.	1/1093614	Equator	1	yes	t <sub>e</sub>
2119	U.S.	1/546807	Equator	2	yes	t <sub>e</sub>

### Transformation of Origin :

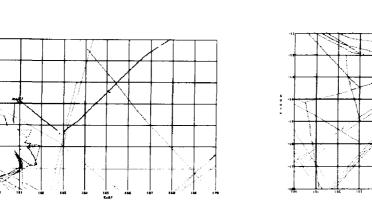
The origin for digitization may be located anywhere on the map. We refer to an origin  $(X_0, Y_0)$  as "standard", if it is at the lower left corner of the map. An origin  $(X_0', Y_0')$  elsewhere on the map is "non-standard". Corresponding to the previous definition of  $c_x$  and  $c_y$  for standard origin,  $c_x'$  and  $c_y'$  are the distances in digitizer counts from a non-standard origin to a digitized sounding of geographical coordinates  $X_1$  and  $Y_1$ .

If a sounding has been digitized with respect to a non-standard origin, it may be related to the standard origin by the use of the following formulas :

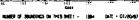
$$c_x = c'_x + 4 \cdot r \cdot s(X'_0 - X_0) \tag{14}$$

$$c_{y} = c_{y}' + \frac{720}{\pi} \cdot r \cdot s \left[ \ln \tan \left\{ \left( \frac{Y_{0}'}{360} + \frac{1}{4} \right) \pi \right\} - \ln \tan \left\{ \left( \frac{Y_{0}}{360} + \frac{1}{4} \right) \pi \right\} \right]$$
(15)

The argument of ln tan in (15) is expressed in radians.



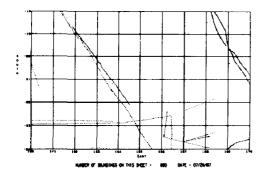
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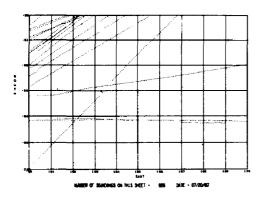
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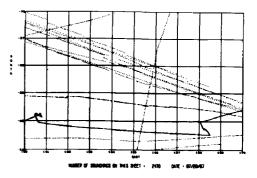


FIG. 7. — Sample page of Appendix B.

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#### APPENDIX B

This appendix contains 708 index sheets of master list No. 4. The sheets are arranged in the following order, according to the Naval Oceanographic Office Plotting Sheet Index Areas :

Low Latitudes	North	(Sheets	0101N — 3614N)
Low Latitudes	South	(Sheets	0201S — 3614S)
High Latitudes	North	(Sheets	0115N - 2418N)
High Latitudes	South	(Sheets	0115S - 2418S)
Areas that do not	contain	any sound	ings are omitted.

#### ACKNOWLEDGEMENTS

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